# The Shapes and Other Properties of Non-Transition Element Complexes. 3. AB5 

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#### Abstract

A qualitative molecular orbital model of the valence electronic structures of pentacoordinate halide complexes $\mathrm{AB}_{5}$ of non-transition elements is developed based on the results of extended Hückel calculations for simple $\mathrm{AB}_{5}$ systems. The model is used to explain the observed trigonal bipyramidal and square pyramidal shapes of $\mathrm{AB}_{5}$ complexes. Variations in bond distances and bond angles are discussed. A simple scheme is used to predict the relative heights of barriers to Berry pseudorotation in trigonal bipyramidal $A B_{5}$ complexes. Barriers to inversion and intramolecular ligand exchange are compared for $A B_{3}$, $A B_{4}$, and $\mathrm{AB}_{5}$ complexes. Relative stabilities of $\mathrm{AB}_{4}, \mathrm{AB}_{5}$, and $\mathrm{AB}_{6}$ complexes are compared and rationalized using molecular orbital correlation diagrams.


In this paper a qualitative molecular orbital (MO) model of electronic structure will be used to explain, rationalize, and predict the structures and other properties of non-transition element complexes of the general formula $\mathrm{AB}_{5}$. This study is limited to those complexes in which the central atom A is of the elements from the main groups 3 through 0 of the periodic table and the ligands B are single atoms, usually halogens. Tables I and II list the known halide complexes. The rules of qualitative MO theory have been discussed elsewhere. ${ }^{1,2}$

In the model presented here the AO basis set consists of the $s$ and $p$ valence $A O$ s of the central atom $A$ and one $A O$ from each ligand B appropriate for the formation of a $\sigma$ bond to the central atom. For $\mathrm{AB}_{5}$ complexes this is a total of nine AOs from which nine MOs can be formed. The valence electrons are counted by including all of those in the valences and $\mathrm{p} A \mathrm{Os}$ of the neutral central atom plus one electron from each halogen ligand (none from oxygen ligands) plus one electron for each negative charge on the complex (subtract positive charges). Comparable studies have been done for the series $\mathrm{AB}_{6}{ }^{2}$ and $\mathrm{AB}_{4}{ }^{3}$

Table I lists the complexes with ten valence electrons. These complexes are mainly trigonal bipyramidal ( $D_{3 h}$ ) in structure with the bonds to the axial ligands ( $\mathrm{A}-\mathrm{B}_{\mathrm{ax}}$ ) being slightly longer than those to the equatorial ligands $\left(\mathrm{A}-\mathrm{B}_{\mathrm{eq}}\right) .{ }^{4-9}$ Table III contains the bond distances that are known for the trigonal bipyramidal ten-electron complexes. Not all ten-electron $\mathrm{AB}_{5}$


complexes have the $D_{3 h}$ structure in one or more phases. For example, although $\mathrm{SbCl}_{5}$ is monomeric and trigonal bipyramidal in the gaseous, liquid, and solid states, ${ }^{8,10,11} \mathrm{PCl}_{5}$ is $D_{3 h}$ in the gas ${ }^{6}$ and in liquid solutions ${ }^{12}$ but in the solid it has the ionic form $\mathrm{PCl}_{4}+\mathrm{PCl}_{6}-{ }^{13}$ Solid $\mathrm{PBr}_{5}$ is $\mathrm{PBr}_{4}+\mathrm{Br}^{-}{ }^{14}$ In the crystalline state $\mathrm{BiF}_{5}{ }^{15.16}$ and $\mathrm{GeF}_{5}{ }^{-17}$ consist of infinite chains of $A B_{5}$ units in which the central atom $A$ is approximately octahedrally coordinated. More serious exceptions to trigonal bipyramidal geometry arise with $\mathrm{InCl}_{5}{ }^{2-}$ and $\mathrm{TlCl}_{5}{ }^{2-}$. ${ }^{18-23}$ In the crystal, isolated $\mathrm{InCl}_{5}{ }^{2-}$ ions occur with square pyramidal geometry ( $C_{4 v}$ ). The bond to the apical chlorine ( $\mathrm{A}-\mathrm{B}_{\mathrm{ap}}$ ) is $2.415 \AA$ and the somewhat longer basal chlorine bonds ( $\mathrm{A}-\mathrm{B}_{\mathrm{ba}}$ ) are $2.456 \AA$. The angle between apical and basal chlorines is $107.87^{\circ}$. The In atom is said to be above the basal plane of the square pyramid, $\mathrm{TlCl}_{5}{ }^{2-}$ is also square pyramidal.

The energy of the square pyramidal ( $C_{4 v}$ ) structure must not be far above that of the trigonal bipyramidal $\left(D_{3 h}\right)$ shape
for the more characteristic members of the ten-electron series. NMR studies of $\mathrm{PF}_{5}, \mathrm{PCl}_{5},{ }^{24} \mathrm{SbCl}_{5}$, and $\mathrm{SiF}_{5}{ }^{-25}$ indicate that all ligands are structurally equivalent on the NMR time scale despite the fact that axial and equatorial ligands are known from other structural studies to occupy positions with different electronic environments. Berry proposed a pseudorotation mechanism of intramolecular ligand exchange to account for the observed NMR equivalence. ${ }^{24}$ In the picture shown here,

the axial ligands 4 and 5 on the left become equatorial on the right while equatorial ligands 2 and 3 become axial. The energy barriers to pseudorotation have been estimated to be on the order of a few $\mathrm{kcal} / \mathrm{mol}$. Other mechanisms for intramolecular ligand exchange have been suggested including a process called the turnstile mechanism. ${ }^{26}$ Here the trigonal bipyramid is assumed to distort to a structure of $C_{s}$ symmetry, then ligands 2,3 , and 4 rotate by $60^{\circ}$ about a pseudothreefold axis, like a turnstile, to another $C_{s}$ structure that can relax to the bipy-

ramidal shape with resulting exchange of axial and equatorial ligands.

A number of mixed ligand complexes are known in the ten-electron bipyramidal $A B_{5}$ series. These include $\mathrm{PF}_{n} \mathrm{Cl}_{5-n},{ }^{27} \mathrm{ClO}_{2} \mathrm{~F}_{3},{ }^{28} \mathrm{IO}_{2} \mathrm{~F}_{3},{ }^{29}$ and $\mathrm{SOF}_{4} .{ }^{30}$ The most stable configuration in each case has the more electronegative ligands in the axial positions. ${ }^{4}$

The 12 -electron $\mathrm{AB}_{5}$ complexes listed in Table II are square pyramidal $\left(C_{4 v}\right)$. The bond to the apical ligand in each of these complexes is $0.1-0.2 \AA$ shorter than the bonds to the basal ligands. The angle between apical and basal ligands is less than $90^{\circ}$, usually around $80^{\circ}$, and the central atom is said to be below the basal plane of the square pyramid, unlike that of the ten-electron square pyramidal structure of $\mathrm{InCl}_{5}{ }^{2-}$. Table IV collects the experimental bond distances and angles. ${ }^{31-35}$ Apical-basal intramolecular ligand exchange has not been observed in the 12 -electron $A B_{5}$ complexes.

Examples of mixed ligand complexes of the 12 -electronseries are $\mathrm{ClOF}_{4}-,{ }^{36} \mathrm{IOF}_{4}{ }^{-},{ }^{37} \mathrm{XeOF}_{4},{ }^{38}$ and $\mathrm{TeOF}_{4}{ }^{2-} .{ }^{39}$ In these complexes the apical position is occupied by the less electronegative ligand.

Table I. Known AB5 Complexes. Ten Valence Electrons

| 3 | 4 | 5 | 6 | 7 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{AlF}_{5}{ }^{2-}$ | $\mathrm{SiF}_{5}{ }^{-}$ | $\mathrm{PF}_{5}$ |  |  |  |
|  | $\mathrm{SiCl}_{5}{ }^{-}$ | $\mathrm{PCl}_{5}$ |  |  |  |
|  |  | $\mathrm{PBr}_{5}$ |  |  |  |
| $\mathrm{GaF}_{5}{ }^{2-}$ | $\mathrm{GeFs}_{5}{ }^{-}$ | $\mathrm{AsF}_{5}$ |  |  |  |
|  | $\mathrm{GeCl}_{5}{ }^{-}$ |  |  |  |  |
| $\begin{aligned} & \mathrm{InF}_{5}{ }^{2-} \\ & \mathrm{InCl}_{5}{ }^{2-} \end{aligned}$ |  | $\mathrm{SbF}_{5}$ $\mathrm{SbCl}_{5}$ |  |  |  |
|  | $\mathrm{SnBr}_{5}-$ | $\mathrm{SbCl}_{5}$ |  |  |  |
|  |  | $\mathrm{BiF}_{5}$ |  |  |  |
| $\mathrm{TlCl}_{5}{ }^{2-}$ |  |  |  |  |  |

Table II. Known $\mathrm{AB}_{5}$ Complexes. 12 Valence Electrons


Table III. Bond Distances ( $\AA$ ) for 10 -Electron $\mathrm{AB}_{5}$ Complexes in the Trigonal Bipyramidal Structure

|  | $\mathrm{SnCl}_{5}{ }^{-a}$ | $\mathrm{PF}_{5}{ }^{b}$ | $\mathrm{PCl}_{5}{ }^{c}$ | $\mathrm{AsF}_{5}{ }^{d}$ | $\mathrm{SbCl}_{5}{ }^{e}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| ${\mathrm{~A}-\mathrm{B}_{\mathrm{ax}}}^{\mathrm{A}-\mathrm{B}_{\text {eq }}}$ | 2.38 | 1.577 | 2.124 | 1.711 | 2.34 |
|  | 2.36 | 1.534 | 2.020 | 1.656 | 2.29 |

${ }^{a}$ Reference 9. ${ }^{b}$ Reference 5. ${ }^{c}$ Reference 6. ${ }^{d}$ Reference 7. ${ }^{e}$ Reference 8.

Table IV. Bond Distances ( $\AA$ ) and Angles (deg) for 12-Electron $\mathrm{AB}_{5}$ Complexes in Square Pyramidal Geometry

|  | $\mathrm{SbF}_{5}^{2-a}$ | $\mathrm{TeF}_{5}{ }^{-b}$ | $\mathrm{IF}_{5}{ }^{c}$ | $\mathrm{XeF}_{5}+d$ | $\mathrm{BrF}_{5}{ }^{c}$ | $\mathrm{SbCl}_{5}{ }^{2-e}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~A}-\mathrm{B}_{\mathrm{ap}}$ | 1.916 | 1.862 | 1.844 | 1.793 | 1.689 | 2.356 |
| $\mathrm{~A}_{\mathrm{b}}$ | 2.075 | 1.953 | 1.869 | 1.845 | 1.774 | 2.636 |
| $\mathrm{~B}_{\mathrm{ap}}-\mathrm{A}-\mathrm{B}_{\mathrm{ba}}$ | 79.4 | 78.9 | 81.9 | 79.0 | 84.8 | 85.2 |

${ }^{a}$ Reference 31. ${ }^{b}$ Reference $32 .{ }^{c}$ Reference 33. ${ }^{d}$ Reference 34.
${ }^{e}$ Reference 35.

The 11 -electron radicals $\mathrm{SF}_{5},{ }^{40} \mathrm{PF}_{5}{ }^{-41}$ and $\mathrm{PCl}_{5}{ }^{-42}$ are known. These are believed to have square pyramidal $C_{40}$ structures.
There have been many theoretical studies of the properties of $\mathrm{AB}_{5}$ species. Hoffmann, Howell, and Meutterties ${ }^{43}$ have already given a qualitative discussion of the properties of the phosphoranes based on the results of extended Hückel calculations for $\mathrm{PH}_{5}$. Their paper is very close in inspiration and in a number of details to the work to be described here but their concern was limited to the ten-electron $\mathrm{AB}_{5}$ series (phosphoranes). Rossi and Hoffmann ${ }^{44}$ have recently published a similar study of transition metals pentacoordinated with ligands such as $\mathrm{CO}, \mathrm{NO}$, and $\mathrm{O}_{2}$, an area completely avoided here. Bartell ${ }^{45 \mathrm{a}}$ and Pearson ${ }^{45 \mathrm{~b}}$ have used a symmetry rule based on the second-order or pseudo-Jahn-Teller effect to compare trigonal bipyramidal and square pyramidal shapes for $\mathrm{AB}_{5}$ complexes. Musher ${ }^{46}$ and Shustorovich and Buslaev ${ }^{47}$ have also presented qualitative studies of $\mathrm{AB}_{5}$ complexes including some limited comparisons with $A B_{4}$ and $A B_{6}$ systems.


Figure 1. MO correlations for $\mathrm{AB}_{5}$ complexes in trigonal bipyramidal $\left(D_{3 h}\right)$ and square pyramidal ( $C_{4 v}$ ) shapes.

The conclusions of a large number of $\mathrm{AB}_{5}$ calculations are remarkably consistent. ${ }^{48-64}$ The 12 -electron $\mathrm{C}_{1} \mathrm{~F}_{5}$ complex is strongly square pyramidal ( $C_{4 v}$ ), not trigonal bipyramidal ( $D_{3 h}$ ). The ten-electron $\mathrm{AB}_{5}$ systems prefer $D_{3 h}$ to $C_{4 v}$ geometry but only by a few $\mathrm{kcal} / \mathrm{mol}$. Calculated bond orders to axial positions in the $D_{3 h}$ structure are smaller than those to equatorial positions and, where geometries were obtained by total energy minimizations, the axial bonds are longer than the equatorial bonds. The calculated charge densities at the axial positions are more negative than those at the equatorial positions, indicating preferred axial sites for substitution of electronegative ligands. When Berry pseudorotation and turnstile mechanisms of intramolecular ligand exchange are compared for the phosphoranes or their analogues the $C_{4 v}$ transition state of the pseudorotation mechanism turns out to be several $\mathrm{kcal} / \mathrm{mol}$ lower than $C_{s}$ structures for the turnstile mechanism. Finally, all of these conclusions appear to be qualitatively insensitive to whether or not central atom d AOs were included in the basis set.

## Molecular Orbitals and Molecular Shapes

AO composition diagrams of the MOs of $D_{3 h}$ geometry are shown in Figure 1. The energy order of the MOs in Figure 1 as well as those in other figures in this paper are given by extended Hückel calculations on model $\mathrm{AH}_{5}$ systems. The lowest energy MO is the bonding orbital $1 \mathrm{a}_{1}{ }^{\prime}$ composed of the central atom s and the ligand AOs all overlapping in phase. The corresponding antibonding MO is $3 \mathrm{a}_{1}{ }^{\prime}$, with all five ligand AOs of opposite phase to that of the central atom s AO making the $3 a_{1}^{\prime}$ orbital high in energy. In $1 a_{2}{ }^{\prime \prime}$ the central atom p AO that points along the threefold axis overlaps in phase the axial ligand AOs. The corresponding antibonding $2 \mathrm{a}_{2}{ }^{\prime \prime} \mathrm{MO}$ has the highest energy in the whole set. A system with a threefold symmetry axis must have doubly degenerate MOs. The lower energy degenerate set $1 e^{\prime}$ is composed of the central atom $p$ AOs that lie in the equatorial plane overlapping in phase with the equatorial ligand AOs. The energy of $1 e^{\prime}$ is higher than that of $1 \mathrm{a}_{2}{ }^{\prime \prime}$ because the overlap between the ligand AOs and the
central atom $p$ orbital is poorer in $1 e^{\prime}$ than it is in $1 a_{2}{ }^{\prime \prime}$. The antibonding $2 \mathrm{e}^{\prime}$ degenerate pair lies high in energy but below $2 \mathrm{a}_{2}{ }^{\prime \prime}$.

Thus far we have formed eight of the nine MOs of the $A B_{5}$ $\left(D_{3 h}\right)$ set. The last MO turns out to have $a_{1}{ }^{\prime}$ symmetry. One way to derive this orbital is by considering the symmetryadapted basis functions of $a_{1}{ }^{\prime}$ symmetry. Symmetry-adapted basis functions have the desired symmetry, in this case $a_{1}{ }^{\prime}$, and they are composed of AO combinations in which only those AOs appear that have coefficients of equal magnitude as required by the symmetry of the group. Once in hand, the sym-metry-adapted basis functions can be linearly combined or mixed to form MOs. There are only three symmetry-adapted functions of $a_{1}{ }^{\prime}$ symmetry: $h_{1}, h_{2}$, and $h_{3}$. From the three $a_{1}{ }^{\prime}$

$h_{1}$

$h_{2}$

$h_{3}$
symmetry-adapted basis functions, linear combinations can produce only three linearly independent $a_{1}{ }^{\prime}$ MOs. In both $1 a_{1}{ }_{1}$ and $3 a_{1}{ }^{\prime}$ we have combined $h_{2}$ and $h_{3}$ in phase with each other, then we mixed that combination either in phase with $h_{1}$ to form $1 a_{1}{ }^{\prime}=h_{1}+h_{2}+h_{3}$, or out of phase with $h_{1}$ to make $3 a_{1}{ }^{\prime}=h_{2}$ $+h_{3}-h_{1}$. (In the MO combinations the symmetry-adapted basis functions do not appear with the same weight, but since we are primarily interested in phase relations we ignore the mixing coefficients that should appear before $h_{1}, h_{2}$, and $h_{3}$.) We already have two MOs with combination $h_{2}+h_{3}$ so the third $\mathrm{a}_{1}{ }^{\prime}$ MO must have $\mathrm{h}_{2}$ and $\mathrm{h}_{3}$ of opposite phase: $\mathrm{h}_{3}-\mathrm{h}_{2}$. But to the out-of-phase combination $h_{3}-h_{2}$ we can match $h_{1}$ either in phase with $h_{3}$ or in phase with $h_{2}$. Thus, we get two possibilities: $a=h_{3}-h_{2}+h_{1}$ and $b=h_{3}-h_{2}-h_{1}$. Either of these combinations looks like the kind of MO that might lie in energy between $1 a_{1}{ }^{\prime}$ and $3 a_{1}{ }^{\prime}$. How do we choose between them? When Hoffmann, Howell, and Muetterties ${ }^{43}$ faced this problem, they added $a$ and $b$ together to make $c$, canceling out

the central atom s AO. Indeed, Rauk, Allen, and Mislow ${ }^{48}$ used a picture like c to represent the corresponding valence MO that they obtained from ab initio calculations for $\mathrm{PH}_{5}$. The choice of $c$ is appealing and, in fact, calculations yield a small central atom s AO coefficient, but that selection would discard some very useful information about $2 a_{1}{ }_{1}$ that makes it different from the related $\mathrm{b}_{1} \mathrm{MO}$ of $C_{4 v}$ geometry. $D_{3 h}$ symmetry allows the central atom s AO to enter $\mathrm{a}_{1}{ }^{\prime}$ MOs and even though its contribution to $2 \mathrm{a}_{1}^{\prime}$ may be small it will directly influence the energy of that MO. On the other hand, the central atom $s$ coefficient of the related $\mathrm{b}_{1} \mathrm{MO}$ of $C_{4 v}$ symmetry must be zero. Figure 1 contains the picture $2 a_{1}{ }^{\prime}(\mathrm{a})$ because of its lower energy and its explicit central atom s AO content. ${ }^{70}$

The $C_{4 v}$ structure is obtained from the $D_{3 h}$ shape by opening the angle between a pair of equatorial ligands from 120 to $180^{\circ}$. This makes the apical-basal angle $90^{\circ}$, simplifies energy comparisons, and serves as a compromise $C_{4 v}$ structure. The MOs of $C_{4 v}$ symmetry develop from those of $D_{3 h}$ geometry. Angular changes that increase AO overlap lower the MO energy. The energy of $1 \mathrm{e}\left(C_{4 v}\right)$ is lower than that of $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)$
because overlap between the central atom p and ligand AO is better in le $\left(C_{4 v}\right)$. The MO energy increases from $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)$ to $2 \mathrm{a}_{1}\left(C_{4 v}\right)$ because a pair of ligand AOs in good overlap with the central atom p AO in one of the components of $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)$ move away from the p orbital lobe toward the MO nodal surface in $2 \mathrm{a}_{1}\left(C_{4 v}\right)$. This is a large change in overlap, and therefore energy, compared to that of $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)-1 \mathrm{e}\left(C_{4 v}\right)$.

The $2 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)-\mathrm{b}_{1}\left(C_{4 v}\right)$ orbital system requires special discussion. The central atom $s$ and one of the equatorial ligand AOs drop out of $2 a_{1}{ }^{\prime}\left(D_{3 h}\right)$ when it becomes $b_{1}\left(C_{4 v}\right)$ and the nodal surfaces move to cut through the base edges of the pyramid and intersect each other along the $\mathrm{C}_{4}$ axis. The alternant phases of the basal ligand AOs of $\mathrm{b}_{1}\left(C_{4 v}\right)$ are the same as those of the axial and equatorial ligand AOs in the $2 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)$ MO to which $b_{1}$ is related. Canceling $A-B$ bonding and antibonding interactions should give $2 a_{1}{ }^{\prime}$ (a) an energy in the nonbonding range and therefore comparable to $b_{1}\left(C_{4 v}\right)$, but whether $2 \mathrm{a}_{1}^{\prime}\left(D_{3 h}\right)$ is above or below $\mathrm{b}_{1}$ is uncertain from qualitative arguments alone. ${ }^{70}$ One might be more confident in saying that $2 \mathrm{a}_{1}{ }^{\prime}(\mathrm{b})$ is higher than $\mathrm{b}_{1}$. Extended Hückel ${ }^{43}$ and ab initio ${ }^{48}$ MO calculations on $A B_{5}$ model systems put $2 a_{1}{ }^{\prime}$ $\left(D_{3 h}\right)$ slightly higher than $\mathrm{b}_{1}\left(C_{4 v}\right)$. The point here is that the energy difference between $2 a_{1}{ }^{\prime}$ and $b_{1}$ is not usually large enough to control the molecular shape of ten-electron $A B_{5}$ complexes for which $2 a_{1}{ }^{\prime}-b_{1}$ is the highest occupied MO. Instead, geometry is primarily determined by the steeply rising $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)-2 \mathrm{a}_{1}\left(C_{4 v}\right)$ MO system just below.

The orbital correlation $3 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)-3 \mathrm{a}_{1}\left(C_{4 v}\right)$ also merits extra consideration. Opening the equatorial angle in $3 a_{1}{ }^{\prime}\left(D_{3 h}\right)$ moves equatorial ligands closer together and increases the overlaps in two pairs of ligand AOs. Although the overlaps themselves are not large, the ligand AO coefficients in $3 a_{1}{ }^{\prime}-3 a_{1}$ are large because of the complicated nature of the nodal surfaces in the orbitals and the large coefficients amplify the overlap change to make $3 \mathrm{a}_{1}\left(C_{4 v}\right)$ considerably lower in energy than $3 \mathrm{a}_{1}^{\prime}\left(D_{3 h}\right)$. However, orbital mixing also acts to stabilize $3 \mathrm{a}_{1}\left(C_{4 v}\right)$ relative to $3 \mathrm{a}_{1}^{\prime}\left(D_{3 h}\right)$. Symmetry eliminates any contribution to $3 a_{1}{ }^{\prime}\left(D_{3 h}\right)$ from the horizontal (equatorial) p AO of the central atom but this AO could add to $3 \mathrm{a}_{1}\left(C_{4 v}\right)$. Similarly, no central atom s orbital can be included in $2 \mathrm{e}^{\prime}$ $\left(D_{3 h}\right)$, although it is allowed in $4 \mathrm{a}_{1}\left(C_{4 v}\right)$. The orbitals $3 \mathrm{a}_{1}$ and $4 \mathrm{a}_{1}\left(C_{4 v}\right)$ are the two highest energy MOs of $\mathrm{a}_{1}$ classification and their AO compositions are different. Therefore, they should be mixed as shown in Figure 2. The after-mixing picture of $3 a_{1}$ is formed by the superposition or summation $3 a_{1}+4 a_{1}$ of before-mixing pictures. Similarly, the after-mixing representation of $4 a_{1}$ is the difference $3 a_{1}-4 a_{1}$ of before-mixing pictures. Mixing makes $3 a_{1}$ an orbital with a large central atom lobe pointing out of the base of the square pyramid and of phase opposite to that of the four basal ligand AOs. The axial ligand $A O$ contribution is reduced but not necessarily to zero as assumed in Figure 2. The perturbation effect of mixing is to lower the energy of $3 a_{1}$ and raise that of $4 a_{1}$. The aftermixing picture of $3 \mathrm{a}_{1}\left(C_{4 v}\right)$ reminds one of the lone pair orbital of the valence shell electron pair repulsion (VSEPR) model. ${ }^{65}$ Mixing also accounts for the higher than expected energy of $4 \mathrm{a}_{1}\left(C_{4 v}\right)$ as shown in Figure 1. On overlap arguments alone one would have expected $4 \mathrm{a}_{1}\left(C_{4 v}\right)$ to be lower than $2 \mathrm{e}^{\prime}$ ( $D_{3 h}$ ).

Consider the correlation diagram of Figure 1 as a whole. For ten-electron $A B_{5}$ complexes the highest occupied MO system is $2 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)-\mathrm{b}_{1}\left(C_{4 v}\right)$. Although the energy slope of this system may favor the square pyramidal structure, the energy difference is not enough to overcome the steeply rising $1 \mathrm{e}^{\prime}$ $\left(D_{3 h}\right)-2 \mathrm{a}_{1}\left(C_{4 v}\right)$ orbital of lower energy. It is the $1 \mathrm{e}^{\prime}-2 \mathrm{a}_{1}$ system that gives the ten-electron $\mathrm{AB}_{5}$ complexes their trigonal bipyramidal geometry. The 12 -electron complexes are square pyramidal because the $3 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)-3 \mathrm{a}_{1}\left(C_{4 v}\right)$ MO system is occupied.


Figure 2. Orbital mixing provides more realistic representations of higher energy $a_{1} \mathrm{MO}$ for square pyramidal geometry.

## The Barrier to Pseudorotation

Ligand exchange has been observed experimentally in a number of ten-electron $A B_{5}$ complexes. If this occurs by the Berry pseudorotation mechanism, and the best evidence indicates that it does, it is because the $C_{4 v}$ transition state is only a few $\mathrm{kcal} / \mathrm{mol}$ above the $D_{3 h}$ structure for these complexes. The source of the pseudorotation barrier is the $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)-2 \mathrm{a}_{1}$ ( $C_{4 v}$ ) MO in Figure 1, but this may be reduced or damped by the $2 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)-\mathrm{b}_{1}\left(C_{4 v}\right)$ system above it. Now $\mathrm{b}_{1}\left(C_{4 v}\right)$ is the only MO of either symmetry that is composed of ligand AOs only and therefore independent of the energy of the central atom orbitals. The choice of a central atom of low electronegativity and therefore high energy AO will raise the energy of $2 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)$ but not $\mathrm{b}_{1}\left(C_{4 v}\right)$. The choice of more electronegative ligands with lower energy AOs will lower $\mathrm{b}_{1}\left(C_{4 v}\right)$ more than it will $2 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)$. Thus by appropriate choices of ligands and central atoms we can control the barrier to pseudorotation. The rules are these: (1) Lower central atom electronegativity lowers the barrier. (2) Greater ligand electronegativity lowers the barrier. Consider the series $\mathrm{PF}_{5}, \mathrm{PCl}_{5}$, $\mathrm{PBr}_{5}$. The ligand electronegativity rises relative to a constant central atom through this series. Since large ligand electronegativity favors a low pseudorotation barrier we predict that the barrier should increase as $\mathrm{PF}_{5}<\mathrm{PCl}_{5}<\mathrm{PBr}_{5}$. Through the series $\mathrm{PF}_{5}, \mathrm{AsF}_{5}, \mathrm{SbF}_{5}$ the electronegativity of the central atom decreases relative to the constant ligand. Since lower central atom electronegativity lowers the barrier, the order of barriers should be $\mathrm{SbF}_{5}<\mathrm{AsF}_{5}<\mathrm{PF}_{5}$. Through the series $\mathrm{SbF}, \mathrm{AsCl}_{5}, \mathrm{PBr}_{5}$ the central atom electronegativities increase and the ligand electronegativities decrease, both raising the barrier. Therefore, we predict the barriers should increase as $\mathrm{SbF}_{5}<\mathrm{AsCl}_{5}<\mathrm{PBr}_{5}$. For the series $\mathrm{PF}_{5}, \mathrm{AsCl}_{5}, \mathrm{SbBr}_{5}$, central atom electronegativities decrease favoring lower barriers while ligand electronegativities also decrease but favoring higher barriers. Because the effects oppose each other, no qualitative predictions are possible in this case.

How do these predictions compare with estimated barriers from experiment? In his original interpretation of NMR data for $\mathrm{PF}_{5}$ and $\mathrm{PCl}_{5}$, Berry ${ }^{24}$ concluded that ligands exchange faster in $\mathrm{PF}_{5}$ than in $\mathrm{PCl}_{5}$ and therefore $\mathrm{PF}_{5}$ must have a lower barrier than does $\mathrm{PCl}_{5}$ or $\mathrm{PF}_{5}<\mathrm{PCl}_{5}$, the order predicted by the qualitative model. Bernstein, Abramowitz, and Levin ${ }^{66}$ have recently published a careful study of the vibrational spectra of $\mathrm{PF}_{5}$ and $\mathrm{AsF}_{5}$ and have calculated the potential functions for axial-equatorial exchange. They find $\mathrm{AsF}_{5}<$ $\mathrm{PF}_{5}$, which agrees with an earlier experimental study by Hoskins and Lord, ${ }^{67}$ and checks the order predicted by the qualitative model. Holmes and co-workers ${ }^{68}$ have publíshed several tables of estimated barriers based on vibrational spectral data and various assumptions. Unfortunately, there are a number of reversals of relative barrier size in Holmes' results but two consistencies remain: $\mathrm{SbCl}_{5}<\mathrm{PCl}_{5}$ and $\mathrm{SbCl}_{5}$ $<\mathrm{AsF}_{5}$. The first pair matches the order that would be pre-


Figure 3. Comparison of higher occupied MOs and barriers to inversion and pseudorotation for $\mathrm{AB}_{3}$ (8e), $\mathrm{AB}_{4}$ (10e), and $\mathrm{AB}_{5}$ (10e) complexes.
dicted by the qualitative model while the second pair presents a comparison the qualitative model cannot make because of opposing effects. In their ab initio SCF MO studies of $\mathrm{PH}_{5}$, Rauk, Allen, and Mislow ${ }^{48}$ performed an additional calculation in which the nuclear charge on the hydrogens was increased from 1.0 to 1.1 , making them slightly more electronegative. The effect was to lower slightly the barrier to pseudorotation compared to that for normal hydrogens. Once more, this is just what the qualitative model predicts would result from increasing the ligand electronegativity. Thus where more rigorous data are available for comparison, the qualitative MO predictions are correct.

One should note that the pseudorotation phenomenon is one of ten-electron $\mathrm{AB}_{5}$ complexes in general and not restricted to group 5 halides. For example, the qualitative model predicts the following increasing order of barriers: $\mathrm{AlF}_{5}{ }^{2-}<\mathrm{SiF}_{5}{ }^{-}<$ $\mathrm{PF}_{5}$. No experimental data are available for comparison.

Is it possible to make the energy of $2 a_{1}{ }^{\prime}\left(D_{3 h}\right)$ so high and that of $\mathrm{b}_{1}\left(C_{4 v}\right)$ so low that the pseudorotation barrier disappears entirely and the ten-electron complex is more stable in square pyramidal form? Among the elements considered here T1 has the highest energy valence $\mathrm{s} A \mathrm{O}$ and combining ligands of lowest energy would yield $\mathrm{T}_{5} \mathrm{~F}_{5}{ }^{2-}$. Unfortunately, this complex is not known but the closely related species $\mathrm{InCl}_{5}{ }^{2-}$ and $\mathrm{TlCl}_{5}{ }^{2-}$ both have square pyramidal shape. Other promising candidates for $C_{4 v}$ structures are $\mathrm{PbFF}_{5}-$ and $\mathrm{PbCl}_{5}{ }^{-}$, but these complexes are unknown.

NMR data indicate that the ten-electron complex $\mathrm{SF}_{4}$ undergoes axial-equatorial ligand exchange through a Berry pseudorotation mechanism. ${ }^{69}$ Barriers must be on the order of a few $\mathrm{kcal} / \mathrm{mol}$, comparable in size to those of the tenelectron $A B_{5}$ series. Although ten-electron $A B_{4}$ and $A B_{5}$ systems are floppy, the eight-electron $A B_{3}$ systems are much more rigid. Figure 3 shows the higher occupied MOs of $A B_{3}$, $A B_{4}$, and $A B_{5}$ in order to compare similarities and differences. The comparison is one between complexes formed from the same central atoms and ligands such as $\mathrm{PF}_{3}, \mathrm{PF}_{4}{ }^{-}$, and $\mathrm{PF}_{5}$. Rauk, Allen, and Mislow ${ }^{48}$ present an ab initio based diagram for $\mathrm{PH}_{3}$ and $\mathrm{PH}_{5}$.

The origin of the inversion barrier is a strikingly similar MO in all three cases. It is the $2 \mathrm{a}_{1}\left(C_{3 v}\right)-1 \mathrm{a}_{2}{ }^{\prime \prime}\left(D_{3 h}\right)$ MO system in $\mathrm{AB}_{3}, 2 \mathrm{a}_{1}\left(C_{2 v}\right)-\mathrm{a}_{2 u}\left(D_{4 h}\right)$ in $\mathrm{AB}_{4}$, and $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)-2 \mathrm{a}_{1}\left(C_{4 v}\right)$ in $A B_{5}$. In each instance the barrier results from ligand $A O s$ moving away from the central atom $\mathrm{p} A O$ that lies along the principal symmetry axis of the transition state. At the top of the barrier, two or more ligands are on or near the nodal surface of the MO. But in the $A B_{4}$ and $A B_{5}$ cases a higher occu-


Figure 4. How MO energies change with distortions of the apical-basal angle $\theta$ on either side of $90^{\circ}$ for the square pyramidal $\mathrm{AB}_{5}$ structure.
pied MO acts to damp or lower the barrier: $3 a_{1}\left(C_{2 v}\right)-b_{1 g}$ ( $D_{4 h}$ ) in $\mathrm{AB}_{4}$ and $2 \mathrm{a}_{1}^{\prime}\left(D_{3 h}\right)-\mathrm{b}_{1}\left(C_{4 v}\right)$ in $\mathrm{AB}_{5}$. Even these damping MOs have much in common. Both $3 \mathrm{a}_{1}\left(\mathrm{AB}_{4}, C_{2 v}\right)$ and $2 \mathrm{a}_{1}{ }^{\prime}\left(\mathrm{AB}_{5}, D_{3 h}\right)$ are nonbonding MOs that include central atom AOs . At the transition state, the orbitals $\mathrm{b}_{1 g}\left(\mathrm{AB}_{4}, D_{4 h}\right)$ and $b_{1}\left(A B_{5}, C_{4 v}\right)$ are identical and involve only ligand $A O s$. This suggests that the ten-electron $A B_{4}$ complexes should follow the same rules as $A B_{5}$ complexes for predicting relative heights of barriers to pseudorotation. No barriers are known for the $A B_{4}$ series. The qualitative MO model cannot predict whether $A B_{4}$ barriers should be higher or lower than those for $A B_{5}$ but it can explain why the $A B_{3}$ complexes, lacking the higher energy barrier-damping MO, should have higher inversion barriers than either $\mathrm{AB}_{4}$ or $\mathrm{AB}_{5}$.

## Bond Distances and Angles and Substituents

The data for ten-electron $\mathrm{AB}_{5}$ complexes in Table III show that the axial $\mathrm{A}-\mathrm{B}$ bonds are slightly longer than the equatorial A-B bonds. The differences are small but consistent. Bond order contributions from individual MOs are proportional to the overlap of AOs on connected atoms multiplied by the product of coefficients of the overlapping AOs. The nodeless MO $1 \mathrm{a}_{1}{ }^{\prime}\left(D_{3 h}\right)$ is smooth and spherical and ligand AO coefficients are practically equal. The $2 a_{1}{ }^{\prime}$ orbital is nearly A-B nonbonding because of the small coefficient of the central atom $\mathrm{s} A O$. Greater differences in bond order occur in the orbitals $1 a_{2}^{\prime \prime}$ ( $\mathrm{A}-\mathrm{B}_{\mathrm{ax}}$ bonding only) and $1 \mathrm{e}^{\prime}$ ( $\mathrm{A}-\mathrm{B}_{\mathrm{eq}}$ bonding only). The $1 \mathrm{e}_{y}{ }^{\prime}$ orbital (viewed below down the threefold axis) has the

same AO composition as $1 a_{2}{ }^{\prime \prime}$, but with each ligand tilted $30^{\circ}$ away from the central atom p axis in $1 \mathrm{e}_{y^{\prime}}$ the overlap is still $87 \%\left(=\cos 30^{\circ}\right)$ of the maximum value that is possible in $1 a_{2}{ }^{\prime \prime}$
( $100 \%$ ). Therefore, one can expect the $\mathrm{A}-\mathrm{B}_{\mathrm{eq}}$ bond order contribution from $1 \mathrm{e}_{y}{ }^{\prime}$ to be about $87 \%$ of the $\mathrm{A}-\mathrm{B}_{\mathrm{ax}}$ contribution of $1 \mathrm{a}_{2}{ }^{\prime \prime}$. But $1 \mathrm{e}_{x}{ }^{\prime}$ also contributes to the $\mathrm{A}-\mathrm{B}_{\mathrm{eq}}$ bond order. Considering the same pair of ligands in $1 \mathrm{e}_{y}{ }^{\prime}$, the corresponding ligand AO 's in $1 \mathrm{e}_{x}{ }^{\prime}$ are $60^{\circ}$ from the central atom p axis, with an overlap that is $50 \%\left(=\cos 60^{\circ}\right)$ of maximum. The $1 \mathrm{e}_{x}{ }^{\prime}$ orbital contains two ligands AOs of the same phase and, therefore, MO normalization requires that the coefficients of those two $A O s$ be smaller in $1 \mathrm{e}_{x}{ }^{\prime}$ than in $1 \mathrm{e}_{y}{ }^{\prime}$. Still, le $\mathrm{e}_{x}{ }^{\prime}$ provides a healthy contribution to the $\mathrm{A}-\mathrm{B}_{\mathrm{eq}}$ bond order. The combined overlap fraction for the $1 \mathrm{e}^{\prime}$ pair is $1.37(=0.87+$ 0.50 ) compared to 1.00 for $1 \mathrm{a}_{2}{ }^{\prime \prime}$, only slightly larger than the ratio of calculated A-B bond order contributions from $1 e^{\prime}$ and $1 \mathrm{a}_{2}{ }^{\prime \prime}$ ( 1.25 for a model $\mathrm{AH}_{5}$ system). Thus, $\mathrm{A}-\mathrm{B}_{\text {eq }}$ bonds are shorter than $\mathrm{A}-\mathrm{B}_{\mathrm{ax}}$ bonds because the two $1 \mathrm{e}^{\prime}$ orbitals combine to give a larger contribution to $A-B_{e q}$ than the single $1 a_{2}{ }^{\prime \prime}$ orbital produces for $A-B_{a x}$.

Calculated charge densities are larger at the axial sites than at the equatorial positions. This is a result of MO orthogonality. Suppose we orthogonalize $2 \mathrm{a}_{1}{ }^{\prime}$ (a) against the spherical blob of $1 a_{1}{ }^{\prime}$. The result requires larger ligand AO coefficients at the axial positions in $2 a_{1}{ }^{\prime}$ (a) than at equatorial positions. Larger coefficients at the axial sites put larger electron densities there. More electronegative substituents prefer positions where coefficients are larger and which offer greater electron density.

In each 12 -electron complex the apical bond is shorter than the basal bonds. The data in Table IV show differences that range from 0.03 to $0.3 \AA$. The highest occupied MO is $3 \mathrm{a}_{1}$ $\left(C_{4 v}\right)$. Look at the after-mixing picture of $3 \mathrm{a}_{1}$ in Figure 2.

Orbital mixing reduces the apical ligand AO coefficient, reducing the $A-B_{a p}$ antibonding nature of $3 a_{1}$. Furthermore, the central atom $p$ AO introduced into $3 a_{1}$ by MO mixing enters in phase with the apical ligand to produce a small bonding component in the $\mathrm{A}-\mathrm{B}_{\mathrm{ap}}$ bond order from $3 \mathrm{a}_{1}$. Thus, $3 a_{1}$ is essentially $A-B_{a p}$ nonbonding but still $A-B_{b a}$ antibonding. The $\mathrm{b}_{1}$ MO makes no contribution to either $\mathrm{A}-\mathrm{B}_{\mathrm{ap}}$ or $\mathrm{A}-\mathrm{B}_{\mathrm{ba}}$ bond orders because this orbital contains no central atom AOs. Compare $2 \mathrm{a}_{1}$ with the two le orbitals. The AO overlaps are exactly the same in the two different kinds of MOs, but there are two ligand AOs in each le orbital but only one ligand AO in $2 \mathrm{a}_{1}$. MO normalization requires smaller AO coefficients where there are more AOs. Therefore, the ligand $A O$ coefficient in $2 a_{1}$ will be larger, making the $A-B_{a p}$ bond order contribution from $2 \mathrm{a}_{1}$ larger than individual $\mathrm{A}-\mathrm{B}_{\mathrm{ba}}$ bond order terms from the 1 e orbitals. In the 12 -electron $\mathrm{AB}_{5}$ complexes $3 a_{1}$ lengthens basal bonds and $2 a_{1}$ shortens the apical bond. For $\mathrm{InCl}_{5}{ }^{2-}$, the ten-electron complex with square pyramidal geometry, the $3 a_{1} \mathrm{MO}$ is vacant but $2 \mathrm{a}_{1}$ still operates to make the axial bond $0.05 \AA$ shorter than the basal bonds.

The $b_{1}$ MO of square pyramidal geometry contains no AO contribution from the apical ligand. The apical coefficient in $3 a_{1}$ (after mixing) is much smaller than those of the basal ligands. Thus, the basal ligand AO coefficients in $b_{1}$ and $3 a_{1}$ increase the electron density at the basal positions compared to that at the apical location. Electronegative substituents, preferring the more electron-rich sites, occupy the basal positions in square pyramidal complexes.

The angles between apical and basal bonds are less than $90^{\circ}$ in square pyramidal 12 -electron complexes. However, in the square pyramidal ten-electron complex $\mathrm{InCl}_{5}{ }^{2-}$ the apicalbasal angle is greater than $90^{\circ}$. Figure 4 shows roughly how the MO energies of $\mathrm{AB}_{5}$ vary as functions of the apical-basal angle $\theta$. The energy of $1 a_{1}$ is nearly constant. The doubly degenerate le levels are at an energy minimum at $\theta=90^{\circ}$, where there is maximum overlap between ligand AOs and the central atom $p$ orbitals that are perpendicular to the $\mathrm{C}_{4}$ axis. Distortions from $90^{\circ}$ produce a symmetric energy increase which is


$A B_{3}$
$A B_{5}$

Figure 5. Comparison of MOs of T -shaped $\mathrm{AB}_{3}$ and square pyramidal $\mathrm{AB}_{5}$.
proportional to the cosine of the angle of distortion from $90^{\circ}$. For a $10^{\circ}$ variation, $\cos 10^{\circ}=0.985$ and the energy is quite small. The $b_{1}$ orbital also has a symmetric energy minimum at $\theta=90^{\circ}$. Variations from $90^{\circ}$ push ligand AOs together out of phase and raise the orbital energy. The slope of the energy curve gets ever steeper the greater the angular variation from $90^{\circ}$ and, thus, $\mathrm{b}_{1}$ limits the amount of distortion in 10 - and 12 -electron complexes. The orbital $2 a_{1}$ has an energy maximum near $\theta=90^{\circ}$ where ligand AOs are near if not on the nodal surface of the MO. For $\theta<90^{\circ}$ all ligand AOs enter $2 a_{1}$ with the same phase; for $\theta>90^{\circ}$ the four basal ligand AOs enter with phase opposite to that of the apical ligand AO. The energy curve of $2 \mathrm{a}_{1}$ is not symmetric. When all ligand AOs have the same phase, normalization requires that their coefficients be smaller than when they have different phases. Since larger coefficients produce larger energy changes, $2 \mathrm{a}_{1}$ has lower energy on the $\theta>90^{\circ}$ side. The angle $\theta=90^{\circ}$ is not an extremum for $3 a_{1}$. The energy of $3 a_{1}$ is high for $\theta>90^{\circ}$ because the basal ligands are in close out-of-phase overlap with the lone pair lobe pointing out of the base of the pyramid. As $\theta$ decreases, these out-of-phase interactions are relaxed and the energy decreases. The slope of this energy decline is steeper where the out-of-phase overlap is greater $\left(\theta>90^{\circ}\right)$.

For ten-electron complexes such as $\operatorname{InCl}_{5}{ }^{2-}\left(\theta=108^{\circ}\right)$, the $2 \mathrm{a}_{1} \mathrm{MO}$ tends to distort the square pyramid toward $\theta>90^{\circ}$. For 12 -electron complexes $3 \mathrm{a}_{1}$ pushes the basal ligands toward $\theta<90^{\circ}$. In both cases $b_{1}$ acts to limit these distortions. The qualitative MO model provides a clear prediction of the direction of the distortion from the flat based pyramid.

## Comparisons with $\mathrm{AB}_{3}, \mathrm{AB}_{4}$, and $\mathrm{AB}_{6}$ Systems

The close similarity between the occupied MOs of T -shaped $\mathrm{AB}_{3}\left(10 \mathrm{e}, C_{2 v}\right)$ and square pyramidal $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$ complexes is shown in Figure 5. Tie lines connect MOs with related AO compositions. The nonbonding $\mathrm{b}_{1}\left(\mathrm{AB}_{5}\right) \mathrm{MO}$ holds the additional electron pair of the square pyramidal complexes. Since $b_{1}\left(A B_{5}\right)$ contains no central atom $A O$ and $b_{1}\left(A B_{3}\right)$ contains no ligand $A O s$, neither of these MOs affects the $A-B$ bond orders of their respective complex series. The contributions to $A-B$ bond order from $1 b_{2}\left(A B_{3}\right)$ and le $\left(A B_{5}\right)$ must be identical because AO compositions and coefficients are identical. The same is roughly true for the two pairs of orbitals $1 a_{1}$ and $2 a_{1}$. Because of the larger number of phase differences in the $3 a_{1}$ orbitals the AO coefficients in these MOs will be larger than those in lower energy orbitals. Therefore, we can


Figure 6. Comparison of MOs of $A B_{4}, A B 5$, and $A B_{6}$ in square planar, square pyramidal, and octahedral shapes.

Table V. Comparison of A-B Distances in $\mathrm{AB}_{5}$ and $\mathrm{AB}_{3}$

|  | $\mathrm{BrF}_{5}{ }^{a}$ | $\mathrm{BrF}_{3}{ }^{b}$ | $\mathrm{XeF}_{5}+c$ | $\mathrm{XeF}_{3}+d$ |
| :--- | :---: | :---: | :---: | :---: |
| A-B (basal or T-crossbar) | 1.774 | 1.810 | 1.845 | 1.89 |
| A-B (apical or T-upright) | 1.689 | 1.721 | 1.793 | 1.83 |

${ }^{a}$ Reference 33. ${ }^{b}$ D. W. Magnuson, J. Chem. Phys., 27, 223 (1957); R. D. Burbank and I. N. Bensey, ibid., 27, 982 (1957). ${ }^{c}$ Reference 34. ${ }^{d}$ D. E. McKee, A. Zalkin, and N. Bartlett, Inorg. Chem., 12, 1713 (1973); P. Boldrini, R. J. Gillespie, P. R. Ireland, and G. J. Schrobilgen, ibid., 13, 1690 (1974).
expect the $3 a_{1}$ MOs to be mainly responsible for differences in $A-B$ bond orders between $A B_{3}$ and $A B_{5}$.

In both $3 a_{1}$ MOs the interactions of the central atom with the basal ( $\mathrm{AB}_{5}$ ) or T-crossbar $\left(\mathrm{AB}_{3}\right)$ ligands are antibonding. In both cases, mixing with a higher $a_{1}$ MO makes $3 a_{1}$ nonbonding between the central atom and the apical $\left(\mathrm{AB}_{5}\right)$ or T-stem or upright $\left(\mathrm{AB}_{3}\right)$ ligands. Because $3 \mathrm{a}_{1}\left(\mathrm{AB}_{3}\right)$ contains fewer ligand $A O$ s than $3 a_{1}\left(\mathrm{AB}_{5}\right)$, MO normalization requires that individual ligand $A O$ coefficients be larger in $3 a_{1}\left(A B_{3}\right)$ than they are in $3 a_{1}\left(A B_{5}\right)$. The differences in magnitudes of ligand $A O$ coefficients and the fact that the $A-B$ interactions are antibonding in both $3 a_{1}$ orbitals results in longer $\mathrm{A}-\mathrm{B}$ bonds for $\mathrm{AB}_{3}\left(10 \mathrm{e}, C_{2 v}\right)$ than for $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$. Table V compares $\mathrm{A}-\mathrm{B}_{\mathrm{ba}}$ with $\mathrm{A}-\mathrm{B}$ (T-crossbar) and $\mathrm{A}-\mathrm{B}_{\mathrm{ap}}$ with $\mathrm{A}-\mathrm{B}$ (T-upright) for the pairs $\mathrm{BrF}_{5}, \mathrm{BrF}_{3}$ and $\mathrm{XeF}_{5}{ }^{+}, \mathrm{XeF}_{3}{ }^{+}$. The less substituted complex has longer bonds. The same trend is to be expected in the following known pairs for which bond distances of one or both members have not been reported: $\mathrm{ClF}_{5}$, $\mathrm{ClF}_{3} ; \mathrm{SeCl}_{5}^{-}, \mathrm{SeCl}_{3}{ }^{-} ; \mathrm{SeBr}_{5}^{-}, \mathrm{SeBr}_{3}{ }^{-}$. A similar lengthening of $\mathrm{A}-\mathrm{B}$ bonds with decreasing substitution for $\mathrm{AB}_{6}\left(14 \mathrm{e}, O_{h}\right)$, $\mathrm{AB}_{4}\left(12 \mathrm{e}, D_{4 h}\right)$, and $\mathrm{AB}_{2}$ (10e, linear) has a related MO explanation. ${ }^{2}$

Figure 6 compares the occupied MOs of $\mathrm{AB}_{4}\left(D_{4 h}\right), \mathrm{AB}_{5}$ $\left(C_{4 v}\right)$, and $\mathrm{AB}_{6}\left(O_{h}\right)$. As front and then rear ligands are added to the square planar system of $\mathrm{AB}_{4}$, the energy of nonbonding $\mathrm{a}_{2 \mathrm{u}}\left(D_{4 h}\right)$ drops to that of bonding $1 \mathrm{t}_{1 u}\left(O_{h}\right)$. The energy of $3 \mathrm{a}_{1}$ $\left(C_{4 v}\right)$ is lower than that of either $2 \mathrm{a}_{1 \mathrm{~g}}\left(D_{4 h}\right)$ or $2 \mathrm{a}_{1 \mathrm{~g}}\left(O_{h}\right)$ because $3 \mathrm{a}_{1}\left(C_{4 v}\right)$ can mix with a higher energy MO of $\mathrm{a}_{1}$ symmetry to reduce out-of-phase A-B overlaps, a process not possible in the higher symmetry $D_{4 h}$ and $O_{h}$ systems where the $2 a_{1 g}$ MOs are the highest energy orbitals of their symmetry. The similar nature of the MOs in Figure 6 suggests that these complexes should be formed from similar elements, That this is true, at least for the $A B_{5}$ and $A B_{6}$ series, can be seen by comparing the pattern of known complexes in Table II with those in related tables in ref 2 and 3 . The highest occupied MOs are A-B antibonding but they have in-phase overlaps between


Figure 7. Comparison of MOs of $\mathrm{AB}_{4}, ~ \mathrm{AB}_{5}$, and $\mathrm{AB}_{6}$ in folded square, trigonal bipyramidal, and octahedral shapes.
ligand AOs, an arrangement that tends to stabilize complexes with large ligands such as iodides compared to fluorides. Exceptions are those complexes in which the central atom is highly electronegative. ${ }^{2}$ Just below the antibonding MO lie nonbonding orbitals which have $\mathrm{B}-\mathrm{B}$ out-of-phase overlaps and no central atom AO. The number of pairs of B-B in-phase overlaps in the antibonding MOs increases from four pairs in $A B_{4}$ to eight pairs in $A B_{5}$ to 12 pairs in $A B_{6}$. The number of pairs of $\mathrm{B}-\mathrm{B}$ out-of-phase interactions in the nonbonding MOs is four pairs each in $A B_{4}$ and $A B_{5}$ and eight pairs in $A B_{6}$. Canceling numbers of in-phase and out-of-phase overlaps in $\mathrm{AB}_{4}\left(12 \mathrm{e}, D_{4 h}\right)$ nearly eliminate the entire class, there being only six known examples and nearly every one of those involves only the most electronegative elements. ${ }^{3}$ There is greater similarity between the $A B_{5}$ and $A B_{6}$ systems with in-phase $\mathrm{B}-\mathrm{B}$ overlaps outnumbering the out-of-phase overlaps. In the ten-electron $\mathrm{AB}_{4}$ complexes of diagonally folded square ( $C_{2 v}$ ) shape, the MO related to $\mathrm{b}_{1 g}\left(\mathrm{AB}_{4}, D_{4 h}\right)$ is empty. These $A B_{4}$ ( $10 \mathrm{e}, C_{2 v}$ ) complexes turn out to have electronic structure and chemical compositions similar to $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$ and $\mathrm{AB}_{6}(14 \mathrm{e}$, $O_{h}$ ).
There are six complexes in the $\mathrm{AB}_{4}\left(12 \mathrm{e}, D_{4 h}\right)$ class, 20 in $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$, and 30 for $\mathrm{AB}_{6}\left(14 \mathrm{e}, O_{h}\right)$. Between $\mathrm{AB}_{5}$ and $A B_{6}$ there are 18 related pairs of complexes composed of the same elements such as $\mathrm{XeF}_{5}{ }^{+}$and $\mathrm{XeF}_{6}$. In other words, for all but two of the known $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$ complexes the related $\mathrm{AB}_{6}\left(14 \mathrm{e}, O_{h}\right)$ complex is also known. The similar electronic structure does favor complexes of the same elements.

Figure 7 compares the occupied MOs of $\mathrm{AB}_{4}\left(C_{2 v}\right), \mathrm{AB}_{5}$ $\left(D_{3 h}\right)$, and $\mathrm{AB}_{6}\left(O_{h}\right)$. There is much less similarity between MOs of these different structures than we found in Figures 5 and 6 . Assuming an angle of $120^{\circ}$ between the equatorial ligands of the diagonally folded square $\left(C_{2 v}\right)$ structure gives $1 b_{2}$ ( $C_{2 v}$ ) and one of the components of $1 \mathrm{e}^{\prime}\left(D_{3 h}\right)$ identical AO compositions, overlaps, and energies.
The $\mathrm{AB}_{4}\left(10 \mathrm{e}, C_{2 v}\right)$ complexes are often reviewed along with those of $A B_{5}\left(10 \mathrm{e}, D_{3 h}\right)$ series, the structure of the $A B_{4}$ complexes being described as trigonal bipyramidal like $A B_{5}$ but with a lone pair of electrons occupying one of the equatorial positions. Despite their geometrical similarity the electronic structures of the two classes of complexes are different enough to make the kinds of complexes contained in the two classes quite different. Consider the differences in the highest occupied MOs at the ten-electron level. In $3 a_{1}\left(\mathrm{AB}_{4}\right)$ the axial and equatorial ligand AOs have the same phase which tend to stabilize complexes with large ligands, iodides more than bromides, etc. See ref 3, Table II. On the other hand, $2 \mathrm{a}_{1}{ }^{\prime}$ $\left(A B_{5}\right)$ has axial and equatorial ligand $A O s$ of opposite phase,





Figure 8. Comparison of MOs of $\mathrm{AB}_{4}$ (folded square) and AB 5 (square pyramidal).
an arrangement stabilized by small ligands and large central atoms, a conclusion supported by the pattern of known tenelectron $\mathrm{AB}_{5}$ complexes shown in Table I. Of the $18 \mathrm{AB}_{5}$ complexes in Table I, there are nine fluorides, seven chlorides, two bromides, and no iodides. The data here are rather sparse. Only $18 \mathrm{AB}_{5}$ complexes with 10 valence electrons are known compared to $32 \mathrm{AB}_{4}$ complexes with 10 electrons. Between these two classes of complexes there are only six related pairs such as $\mathrm{PF}_{4}{ }^{-}, \mathrm{PF}_{5}$.

Figure 8 compares the electronic structures of $\mathrm{AB}_{4}(10 \mathrm{e}$, $\left.C_{2 v}\right)$ and $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$ complexes. In both classes of complexes the highest occupied MO is A-B antibonding but with $\mathrm{B}-\mathrm{B}$ in-phase overlaps which favor large ligands. In each class the antibonding $3 \mathrm{a}_{1} \mathrm{MO}$ is stabilized by mixing with a higher unoccupied orbital to the same symmetry to form an orbital related to the lone pair orbital of the VSEPR model. The similarity of highest occupied MOs suggests that the two classes of complexes should be formed from similar elements. Between 32 known $\mathrm{AB}_{4}\left(10 \mathrm{e}, C_{2 v}\right)$ complexes and 20 known $\mathrm{AB}_{5}\left(12 \mathrm{e}, C_{4 v}\right)$ complexes, there are 19 related pairs, such as $\mathrm{SF}_{4}$ and $\mathrm{SF}_{5}{ }^{-}$.

## Summary

Molecular orbitals and their relative energies can be obtained qualitatively following some simple rules. The results can be supported by MO calculations. The MO energies show that 12 -electron $A B_{5}$ complexes are square pyramidal. The ten-electron series should be trigonal bipyramidal, although some square pyramidal exceptions are known. These exceptions can be understood with a model that also predicts the relative heights of barriers to pseudorotation in the trigonal bipyramidal complexes. Energy level comparisons are made to show the relationship of pseudorotation or inversion barriers in $A B_{3}$, $A B_{4}$, and $A B_{5}$ complexes. Qualitative bond order arguments rationalize the longer axial bonds in trigonal bipyramidal complexes and the shorter apical bonds in square pyramidal structures. Similar reasoning, including MO normalization requirements, explains why $\mathrm{Br}-\mathrm{F}$ bonds are shorter in $\mathrm{BrF}_{5}$ than in $\mathrm{BrF}_{3}$. Qualitative charge density arguments explain why more electronegative ligands prefer axial sites in trigonal bipyramidal complexes and basal positions in square pyramidal structures. Relative stabilities of complexes can be interpreted by considering the properties of the higher occupied MOs. Stabilities of $\mathrm{AB}_{5}$ complexes can be compared to those of re-
lated series in the $A B_{4}$ and $A B_{6}$ classes. Qualitative MO theory can act as a great organizing principle for a large body of inorganic chemistry.

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(70) Note Added in Proof. R. Hoffmann and E. Shustorovich (private communlcatlon) point out that the ratlo of sizes of axial and equatorial Ilgand orbital coefficients in a is $3 / 2$ from first-order perturbation theory. Thls ratlo just compensates for the $2 / 3$ ratio of numbers of $A-B_{a x}$ out of phase to $A-B_{e q}$ In phase interactions In a.

